

Formulas for Tesla Coils

v. 3.3

Ohm's Laws

$$V = I \times R = P / I = \text{SQRT}(P \times R)$$

$$I = V / R = \text{SQRT}(P / R) = P / V$$

$$R = V / I = P / (I^2) = V^2 / P$$

$$P = I \times V = I^2 \times R = V^2 / R$$

Where:

V = Voltage in Volts

I = Current in Amps

R = Resistance in Ohms

P = Power in Watts

Resonate Frequency

$$F_o = 1 / (2 \times \pi \times \text{SQRT}(L \times C))$$

Where:

F_o = Resonant frequency in Hertz

π = 3.14159...

SQRT = Square root function

L = Inductance in Henries

C = Capacitance in Farads

Reactance

$$X_L = 2 \times \pi \times F \times L$$

$$X_C = 1 / (2 \times \pi \times F \times C)$$

Where:

X_L = Inductive reactance in Ohms

X_C = Capacitive reactance in Ohms

π = 3.14159...

F = Frequency in Hertz
L = Inductance in Henries
C = Capacitance in Farads

RMS

$$V_{\text{peak}} = V_{\text{rms}} \times \text{SQRT}(2) \quad \text{For sine waves only}$$

Where:

V_{peak} = Peak voltage in volts
 V_{rms} = RMS voltage in Volts RMS
SQRT = Square root function

Energy

$$E = 1/2 \times C \times V^2 = 1/2 \times L \times I^2$$

Where:

E = Energy in Joules
L = Inductance in Henries
C = Capacitance in Farads
V = Voltage in Volts
I = Current in Amps

Power

$$P = E / t = E \times \text{BPS}$$

Where:

P = Power in Watts
E = Energy in Joules
t = Time in Seconds
BPS = The break rate (120 or 100 BPS)

Helical Coil

$$L_h = (N \times R)^2 / (9 \times R + 10 \times H)$$

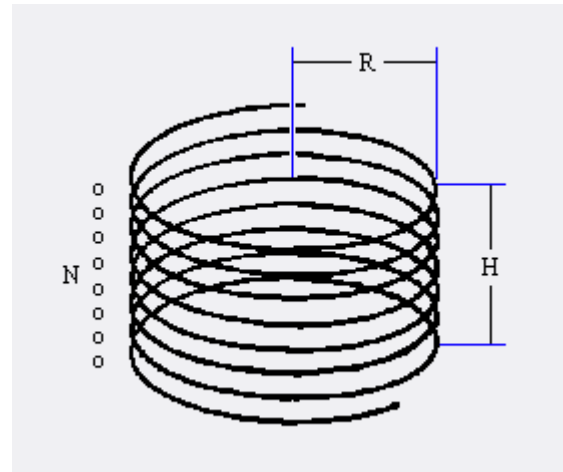
Where:

L_h = Inductance in micro-Henries

N = number of turns

R = Radius in inches

H = Height in inches



Flat spiral

$$L_f = (N \times R)^2 / (8 \times R + 11 \times W)$$

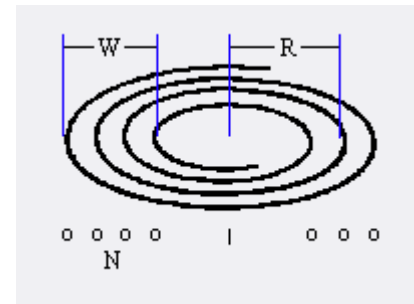
Where:

L_f = Inductance in micro-Henries

N = number of turns

R = Average radius in inches

W = Width in inches



Conical Primary

$$L_1 = (N \times R)^2 / (9 \times R + 10 \times H)$$

$$L_2 = (N \times R)^2 / (8 \times R + 11 \times W)$$

$$L_c = \text{SQRT}(((L_1 \times \sin(x))^2 + (L_2 \times \cos(x))^2) / (\sin(x) + \cos(x)))$$

Where:

L_c = Inductance in Microhenries

L_1 = helix factor

L_2 = spiral factor

SQRT = Square root function

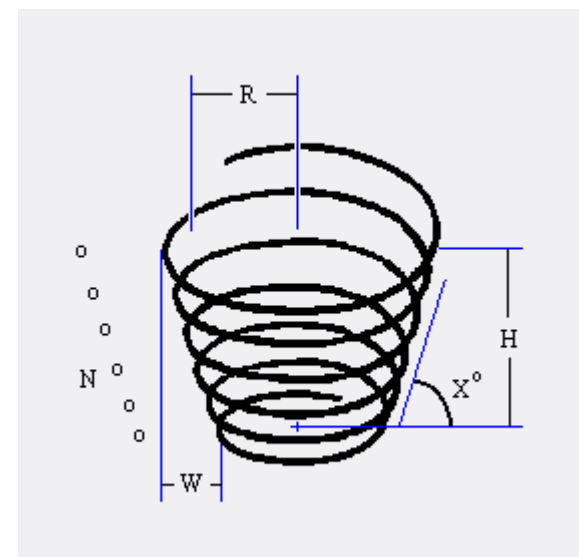
N = number of turns

R = average radius of coil in inches

H = effective height of the coil in inches

W = effective width of the coil in inches

X = rise angle of the coil in degrees



Resonant Primary Capacitance

$$C_{res} = I / (2 \times \pi \times f_l \times V)$$

Where:

C_{res} = Resonant capacitor value in Farads

I = NST rate current in Amps

π = 3.14159...

f_l = AC line frequency in Hertz

V = NST rated voltage in Volts

Static Gap Primary LTR Capacitance

$$C_{ltr} = I / (4 \times f_l \times V)$$

Where:

C_{ltr} = The LTR cap size in Farads

I = NST rate current in Amps

f_l = AC line frequency in Hertz

V = NST rated voltage in Volts

Sync Gap Primary LTR Capacitance

$$C_{ltr} = 0.83 \times I / (BPS \times V)$$

Where:

C_{ltr} = The LTR cap size in Farads

I = The NST rated current in Amps

V = The NST rated voltage in Volts

BPS = The break rate (120 or 100 BPS)

Top Voltage

$$V_t = V_f \times \text{SQRT}(L_s / (2 \times L_p))$$

Where:

V_t = Peak top voltage in Volts

Vf = gap firing voltage in Volts
SQRT = Square root function
Ls = Secondary inductance in Heneries
Lp = Primary inductance in Heneries

PFC Capacitors

$$C_{pfc} = V_o \times I_o / (2 \times \pi \times F_l \times V_i^2)$$

Where:

C_{pfc} = Power factor correction capacitance in Farads

V_o = NST output voltage in Volts

I_o = NST output current in Amps

π = 3.14159...

F_l = AC line frequency in Hertz

V_i = NST input voltage in Volts

Power-BPS

$$P = BPS \times 1/2 \times C_p \times V_f^2$$

Where:

P = Coil power in Watts

BPS = Breaks per second

C_p = Primary capacitance in Farads

V_f = Gap firing Voltage

Transformers

$$V_i \times I_i = V_o \times I_o$$

Where:

V_i = Input voltage in Volts

I_i = Input current in Amps

V_o = Output voltage in Volts

I_o = Output current in Amps

Primary Peak Current

$$I_{Ppeak} = V_f \times \text{SQRT}(C_p / L_p)$$

Where:

I_{Ppeak} = Peak primary loop current Amps

V_f = Firing Voltage in Volts

SQRT = Square root function

L_p = Primary inductance in Heneries

C_p = Primary capacitance in Farads

Surge Impedance

$$Z_s = \text{SQRT}(L_p / C_p)$$

Where:

Z_s = Surge impedance in Ohms

SQRT = Square root function

L_p = Primary inductance in Heneries

C_p = Primary capacitance in Farads

Secondary "Q" Factor

$$Q = 2 \times \pi \times F_o \times L_s / R_{ac} = \text{SQRT}(L_s / C_s) / R_{ac}$$

Where:

Q = "Q" factor

F_o = Fundamental frequency in Hertz

L_s = Secondary inductance in Heneries

C_s = Secondary capacitance in Farads

R_{ac} = Secondary "AC" resitance in Ohms

SQRT = Square root function

Freau Spark Length Formula

$$L = 1.7 \times \text{SQRT}(P)$$

L = Maximum spark length in Inches

SQRT = Square root function

P = Wallplug Watts

Appendix

Wire Chart

| Gauge No. B. & S. | Diam in Mils ¹ | Circular Mil Area | Turns Per Linear Inch ² | Feet per Lb. | | Ohms per 1000ft. 250 C. | Current Carrying Capacity @ 1500 C.M. per Amp ³ | Diameter in mm |
|----------------------|---------------------------|----------------------|---------------------------------------|--------------|--------|----------------------------|--|----------------|
| | | | Enamel | Bare | Enamel | | | |
| 1 | 289.3 | 82690 | - | 3.95 | - | 0.13 | 55.7 | 7.35 |
| 2 | 257.6 | 66370 | - | 4.98 | - | 0.16 | 44.1 | 6.54 |
| 3 | 229.4 | 52640 | - | 6.27 | - | 0.2 | 35.0 | 5.83 |
| 4 | 204.3 | 41740 | - | 7.91 | - | 0.25 | 27.7 | 5.19 |
| 5 | 181.9 | 33100 | - | 9.980 | - | 0.32 | 22.0 | 4.62 |
| 6 | 162.0 | 26250 | - | 12.58 | - | 0.4 | 17.5 | 4.12 |
| 7 | 144.3 | 20820 | - | 15.87 | - | 0.5080 | 13.8 | 3.665 |
| 8 | 128.5 | 16510 | 7.6 | 20.01 | 19.6 | 0.64 | 11.0 | 3.264 |
| 9 | 114.4 | 13090 | 8.6 | 25.23 | 25 | 0.81 | 8.7 | 2.906 |
| 10 | 101.90 | 10380 | 9.6 | 31.82 | 31.5 | 1.02 | 6.9 | 2.588 |
| 11 | 90.74 | 8234 | 10.7 | 40.12 | 39 | 1.28 | 5.5 | 2.305 |
| 12 | 80.81 | 6530 | 12.0 | 50.59 | 49.9 | 1.62 | 4.4 | 2.053 |
| 13 | 71.96 | 5178 | 13.5 | 63.8 | 62.9 | 2.04 | 3.5 | 1.828 |
| 14 | 64.08 | 4107 | 15.0 | 80.44 | 79.94 | 2.58 | 2.7 | 1.628 |
| 15 | 57.07 | 3257 | 16.8 | 101.4 | 100.4 | 3.25 | 2.2 | 1.450 |
| 16 | 50.82 | 2583 | 18.9 | 127.9 | 126.8 | 4.09 | 1.7 | 1.291 |
| 17 | 45.26 | 2048 | 21.2 | 161.3 | 159.4 | 5.16 | 1.3 | 1.150 |
| 18 | 40.30 | 1624 | 23.6 | 203.4 | 201.1 | 6.51 | 1.1 | 1.024 |
| 19 | 35.89 | 1288 | 26.4 | 256.5 | 253.2 | 8.21 | 0.86 | 0.91 |
| 20 | 31.96 | 1022 | 29.4 | 323.4 | 318.4 | 10.35 | 0.68 | 0.81 |
| 21 | 28.46 | 810.1 | 33.1 | 407.8 | 400.6 | 13.05 | 0.54 | 0.72 |
| 22 | 25.35 | 642.4 | 37.0 | 514.2 | 507.1 | 16.46 | 0.43 | 0.64 |
| 23 | 22.57 | 509.5 | 41.3 | 648.4 | 633.7 | 20.76 | 0.34 | 0.57 |
| 24 | 20.10 | 404.0 | 46.3 | 817.7 | 804.5 | 26.17 | 0.27 | 0.51 |
| 25 | 17.90 | 320.4 | 51.7 | 1031 | 1010 | 33.0 | 0.21 | 0.45 |
| 26 | 15.94 | 254.1 | 58.0 | 1300 | 1279 | 41.62 | 0.17 | 0.4 |
| 27 | 14.20 | 201.5 | 64.9 | 1639 | 1600 | 52.48 | 0.13 | 0.36 |
| 28 | 12.64 | 159.8 | 72.7 | 2067 | 2028 | 66.17 | 0.11 | 0.32 |
| 29 | 11.26 | 126.7 | 81.6 | 2607 | 2513 | 83.44 | 0.08 | 0.29 |
| 30 | 10.03 | 100.5 | 90.5 | 3287 | 3208 | 105.2 | 0.07 | 0.25 |
| 31 | 8.928 | 79.70 | 101 | 4170 | 4052 | 132.7 | 0.05 | 0.23 |
| 32 | 7.950 | 63.21 | 113 | 5160 | 4995 | 167.3 | 0.04 | 0.2 |
| 33 | 7.080 | 50.13 | 127 | 6550 | 6337 | 211.0 | 0.03 | 0.18 |
| 34 | 6.305 | 29.75 | 143 | 8320 | 8055 | 266.0 | 0.03 | 0.16 |
| 35 | 5.615 | 31.52 | 158 | 10500 | 10250 | 335.0 | 0.02 | 0.14 |
| 36 | 5.000 | 25.00 | 175 | 13200 | 12800 | 423.0 | 0.02 | 0.13 |
| 37 | 4.453 | 19.83 | 198 | 16300 | 15750 | 533.4 | 0.01 | 0.11 |
| 38 | 3.965 | 15.72 | 224 | 20600 | 20020 | 672.6 | 0.01 | 0.1 |
| 39 | 3.531 | 12.47 | 284 | 27000 | 26240 | 848.1 | 0.01 | 0.09 |
| 40 | 3.145 | 9.88 | 282 | 34400 | 33330 | 1069 | 0.01 | 0.08 |

Capacitor Chart

MMC Capacitor Chart

Capacitor Value (uF)

| NST Type | 60Hz | | | 50Hz | | |
|----------|----------|----------------|--------------|----------|----------------|--------------|
| | Resonant | Static Gap LTR | Sync Gap LTR | Resonant | Static Gap LTR | Sync Gap LTR |
| 7.5/30 | 0.0106 | 0.0159 | 0.0277 | 0.0127 | 0.0191 | 0.0332 |
| 7.5/60 | 0.0212 | 0.0318 | 0.0533 | 0.0256 | 0.0382 | 0.0664 |
| 7.5/90 | 0.0318 | 0.0477 | 0.0830 | 0.0382 | 0.0573 | 0.0996 |
| 7.5/120 | 0.0424 | 0.0637 | 0.1107 | 0.0509 | 0.0764 | 0.1328 |
| 9/30 | 0.0088 | 0.0133 | 0.0231 | 0.0106 | 0.0159 | 0.0277 |
| 9/60 | 0.0177 | 0.0265 | 0.0461 | 0.0212 | 0.0318 | 0.0553 |
| 9/90 | 0.0265 | 0.0398 | 0.0692 | 0.0318 | 0.0477 | 0.0830 |
| 9/120 | 0.0354 | 0.0531 | 0.0922 | 0.0424 | 0.0637 | 0.1107 |
| 10/23 | 0.0061 | 0.0092 | 0.0159 | 0.0073 | 0.0110 | 0.0191 |
| 12/30 | 0.0066 | 0.0099 | 0.0173 | 0.0080 | 0.0119 | 0.0208 |
| 12/60 | 0.0133 | 0.0199 | 0.0346 | 0.0159 | 0.0239 | 0.0415 |
| 12/90 | 0.0199 | 0.0298 | 0.0519 | 0.0239 | 0.0358 | 0.0623 |
| 12/120 | 0.0265 | 0.0398 | 0.0692 | 0.0318 | 0.0477 | 0.0830 |
| 15/30 | 0.0053 | 0.0080 | 0.0138 | 0.0064 | 0.0096 | 0.0166 |
| 15/60 | 0.0106 | 0.0159 | 0.0277 | 0.0127 | 0.0191 | 0.0332 |
| 15/90 | 0.0159 | 0.0239 | 0.0415 | 0.0191 | 0.0286 | 0.0496 |
| 15/120 | 0.0212 | 0.0318 | 0.0553 | 0.0255 | 0.0382 | 0.0664 |

Warning!! Never use "Resonant" cap values anymore!!! Use "LTR" instead to keep from damaging NSTs!!!

Metric Prefixes

| Prefix | Symbol | Decimal | Exponential |
|--------|--------|----------------|-------------|
| pico | p | 0.000000000001 | 1e-12 |
| nano | n | 0.000000001 | 1e-9 |
| micro | u | 0.000001 | 1e-6 |
| milli | m | 0.001 | 1e-3 |
| kilo | k | 1000.0 | 1e+3 |
| Mega | M | 1,000,000 | 1e+6 |
| Giga | G | 1,000,000,000 | 1e+9 |

Cornell Dubilier 942 Series polypropylene Metal Foil Caps (Recommended)

| Part Number | Cap. μ F | D inches (mm) | L inches (mm) | d inches (mm) | Typical ESR milli Ω ms | Typical ESL nH | dV/dt V/ μ s | I Peak A | IRMS A |
|-------------|--------------|---------------|---------------|---------------|-------------------------------|----------------|------------------|----------|--------|
| 942C20S1K | 0.01 | 0.472 (12.0) | 1.339 (34.0) | 0.040 (1.0) | 50 | 20 | 5137 | 51 | 2.2 |
| 942C20S15K | 0.015 | 0.571 (14.5) | 1.339 (34.0) | 0.040 (1.0) | 40 | 21 | 5137 | 77 | 2.8 |
| 942C20S22K | 0.022 | 0.650 (16.5) | 1.339 (34.0) | 0.040 (1.0) | 20 | 22 | 5137 | 113 | 4.2 |
| 942C20S33K | 0.033 | 0.768 (19.5) | 1.339 (34.0) | 0.040 (1.0) | 12 | 23 | 5137 | 170 | 6.0 |
| 942C20S47K | 0.047 | 0.709 (18.0) | 1.811 (46.0) | 0.040 (1.0) | 10 | 28 | 2879 | 135 | 7.1 |
| 942C20S68K | 0.068 | 0.807 (20.5) | 1.811 (46.0) | 0.040 (1.0) | 6 | 29 | 2879 | 196 | 9.9 |
| 942C20P1K | 0.1 | 0.965 (24.5) | 1.811 (46.0) | 0.047 (1.2) | 5 | 30 | 2879 | 288 | 12.1 |
| 942C20P15K | 0.15 | 1.161 (29.5) | 1.811 (46.0) | 0.047 (1.2) | 5 | 32 | 2879 | 432 | 13.5 |

Metal Foil caps are normally the best type to use for MMCs.

Cornell Dubilier 940 Series polypropylene Metal Film Caps

| Part Number | Cap. μ F | Vdc | Vac | D inches (mm) | L inches (mm) | d inches (mm) | Typical ESR milli Ω ms | Typical ESL nH | dV/dt V/ μ s | I Peak A | IRMS A |
|-------------|--------------|------|-----|---------------|---------------|---------------|-------------------------------|----------------|------------------|----------|--------|
| 940C20S22K | 0.022 | 2000 | 630 | 0.453 (11.5) | 1.339 (34.0) | 0.040 (1.0) | 35 | 6 | 1712 | 38 | 2.6 |
| 940C20S33K | 0.033 | 2000 | 630 | 0.531 (13.5) | 1.339 (34.0) | 0.040 (1.0) | 20 | 21 | 1712 | 57 | 3.8 |
| 940C20S47K | 0.047 | 2000 | 630 | 0.591 (15.0) | 1.339 (34.0) | 0.040 (1.0) | 12 | 22 | 1712 | 80 | 5.2 |
| 940C20S68K | 0.068 | 2000 | 630 | 0.689 (17.5) | 1.339 (34.0) | 0.040 (1.0) | 8 | 23 | 1712 | 116 | 6.9 |
| 940C20P1K | 0.1 | 2000 | 630 | 0.827 (21.0) | 1.339 (34.0) | 0.040 (1.0) | 7 | 24 | 1712 | 171 | 8.3 |
| 940C20P15K | 0.15 | 2000 | 630 | 0.768 (19.5) | 1.811 (46.0) | 0.040 (1.0) | 7 | 29 | 960 | 144 | 8.9 |
| 940C20P22K | 0.22 | 2000 | 630 | 0.866 (22.0) | 1.811 (46.0) | 0.040 (1.0) | 8 | 30 | 960 | 211 | 9.0 |
| 940C20P33K | 0.33 | 2000 | 630 | 1.063 (27.0) | 1.811 (46.0) | 0.047 (1.2) | 8 | 32 | 960 | 317 | 10.1 |
| 940C20P47K | 0.47 | 2000 | 630 | 1.260 (32.0) | 1.811 (46.0) | 0.047 (1.2) | 6 | 34 | 960 | 451 | 13.0 |
| 940C20P56K | 0.56 | 2000 | 630 | 1.220 (31.0) | 2.126 (54.0) | 0.047 (1.2) | 7 | 37 | 754 | 422 | 12.6 |
| 940C20P68K | 0.68 | 2000 | 630 | 1.339 (34.0) | 2.126 (54.0) | 0.047 (1.2) | 6 | 39 | 754 | 513 | 14.3 |
| 940C20W1K | 1 | 2000 | 630 | 1.614 (41.0) | 2.126 (54.0) | 0.047 (1.2) | 5 | 42 | 754 | 754 | 17.7 |

Metal Film caps are normally not recommended for MMCs unless the primary peak current is well within the capacitor's ability.

McMaster Carr's Polycarbonate tubing cut to length:

| ID | OD | Part# | Per Foot |
|--------|--------|---------|----------|
| 1" | 1-1/4" | 8585K15 | \$4.58 |
| 1-1/4" | 1-1/2" | 8585K16 | 5.32 |
| 1-3/8" | 1-1/2" | 8585K43 | 3.24 |
| 1-1/2" | 1-3/4" | 8585K17 | 6.51 |
| 1-3/4" | 2" | 8585K18 | 7.00 |
| 2" | 2-1/4" | 8585K46 | 8.19 |
| 2-1/4" | 2-1/2" | 8585K19 | 8.73 |
| 2-1/2" | 2-3/4" | 8585K34 | 10.01 |
| 2-3/4" | 3" | 8585K21 | 10.70 |
| 3-1/4" | 3-1/2" | 8585K33 | 13.25 |
| 3-3/4" | 4" | 8585K22 | 17.06 |
| 4-3/4" | 5" | 8585K45 | 24.38 |
| 5-3/4" | 6" | 8585K23 | 29.92 |
| 7-3/4" | 8" | 8585K48 | 33.36 |

Magnet Wire

Great for use in motors, transformers, relays, and other high-speed winding applications. Wire is made of solid copper and has a clear enamel coating that gives it good resistance to moisture and heat, so it can be used in hermetic motors. Maximum temperature is 392° F. Meets NEMA 1000 MW-73 and MW-35. UL recognized.

Wire OD: 36 AWG is 0.006", 34 AWG is 0.008", 32 AWG is 0.010", 30 AWG is 0.012", 28 AWG is 0.014", 26 AWG is 0.018", 24 AWG is 0.022", 22 AWG is 0.028", 20 AWG is 0.035", and 18 AWG is 0.043".



| AWG | Spool Lg., ft. | Per Spool | AWG | Spool Lg., ft. | Per Spool |
|-----|----------------|---------------------------------|-----|----------------|---------------------------------|
| 36 | 12,300 | 7588K85 \$20.61 | 26 | 1,500 | 7588K75 \$11.54 |
| 36 | 24,600 | 7588K84 41.20 | 26 | 3,000 | 7588K55 22.09 |
| 34 | 7,800 | 7588K87 19.36 | 24 | 792 | 7588K77 11.19 |
| 34 | 15,600 | 7588K86 41.98 | 24 | 2,000 | 7588K57 22.11 |
| 32 | 4,350 | 7588K89 18.51 | 22 | 750 | 7588K79 12.75 |
| 32 | 8,700 | 7588K88 35.15 | 22 | 1,500 | 7588K59 25.49 |
| 30 | 3,000 | 7588K71 14.88 | 20 | 500 | 7588K81 16.73 |
| 30 | 6,000 | 7588K51 28.27 | 20 | 900 | 7588K61 25.08 |
| 28 | 2,000 | 7588K73 13.05 | 18 | 300 | 7588K83 12.30 |
| 28 | 4,000 | 7588K53 24.78 | 18 | 600 | 7588K63 24.59 |